# **Graph Representation Learning for Drug Discovery**

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# **The Process of Drug Discovery**

- A very long and costly process
  - On average takes more than 10 years and \$2.5B to get a drug approved



#### **Molecules }** The state (Ž× $\neg \bigcirc$ $\overline{\mathbf{Q}}$ 0-4 \$ \_\_\_\_{ $\mathcal{P}$ $\int$ $\sim \sim \sim$

#### **Research Problems**



# **Molecule Properties Prediction**

- Predicting the properties of molecules or compounds is a fundamental problem in drug discovery
  - E.g., in the stage of virtual screening
- Each molecule is represented as a graph
- The fundamental problem: how to represent a whole molecule (graph)



# **Graph Neural Networks**

- Techniques for learning node/graph representations
  - Graph convolutional Networks (Kipf et al. 2016)
  - Graph attention networks (Veličković et al. 2017)
- Neural Message Passing (Gilmer et al. 2017)

**MESSAGE PASSING:**  $M_k(h_v^k, h_w^k, e_{vw})$ 

**AGGREGATE**:  $m_v^{k+1} = \text{AGGREGATE}\{M_k(h_v^k, h_w^k, e_{vw}): w \in N(v)\}$ 

**COMBINE**:  $h_v^{k+1} = \text{COMBINE}(h_v^k, m_v^{k+1})$ 

**READOUT:**  $g = \text{READOUT}\{h_v^K : v \in G\}$ 



#### InfoGraph: Unsupervised and Semi-supervised Whole-Graph Representation Learning (Sun et al. ICLR'20)

- For supervised methods based on graph neural networks, a large number of labeled data are required for training
- The number of labeled data are very limited in drug discovery
  - A large amount of unlabeled data (molecules) are available
- This work: how to effectively learn whole graph representations in unsupervised or semi-supervised fashion

Fanyun Sun, Jordan Hoffman, Vikas Verma and Jian Tang. InfoGraph: Unsupervised and Semi-supervised Graph-Level Representation Learning via Mutual Information Maximization. ICLR'20.

#### InfoGraph: Unsupervised Whole-Graph Representation Learning (Sun et al. ICLR'20)

- Maximizing the **mutual information** between the whole graph representation  $H_{\varphi}(G)$  and all the sub-structure representation  $h_{\varphi}^{i}$ .
  - Ensure the graph representation capture the predominant information among all the substructures
- K-layer graph neural networks:

 $h_{v}^{(k)} = \text{COMBINE}^{(k)} h_{v}^{(k-1)}, \text{AGGREGATE}^{(k)} h_{v}^{(k-1)}, h_{u}^{(k-1)}, e_{uv} : u 2 N(v)$ 

- Summarize the local structure information at every node *i*:  $h_{\varphi}^{i} = \text{CONCAT}(\{h_{i}^{(k)}\}_{k=1}^{K})$
- Summarize the information of the whole graph:

$$H_{\varphi}(G) = \text{READOUT}(\{h_{\varphi}^{i}\}_{i=1}^{N})$$

Fanyun Sun, Jordan Hoffman, Vikas Verma and Jian Tang. InfoGraph: Unsupervised and Semi-supervised Graph-Level Representation Learning via Mutual Information Maximization. ICLR'20.

# **InfoGraph: Unsupervised Whole-Graph Representation Learning**

• Maximizing the **mutual information** between the whole graph representation  $H_{\varphi}(G)$  and all the sub-structure representation  $\vec{h}_{\phi}^{u}$ 

$$\hat{\phi}, \hat{\psi} = \operatorname*{arg\,max}_{\phi,\psi} \sum_{G \in \mathbf{G}} \frac{1}{|G|} \sum_{u \in G} I_{\phi,\psi}(\vec{h}^u_\phi; H_\phi(G)).$$

• We use the Jensen-Shannon MI estimator:

 $I_{\phi,\psi}(h^i_{\phi}(G);H_{\phi}(G)):=$ 

 $\mathbb{E}_{\mathbb{P}}[-\operatorname{sp}(-T_{\phi,\psi}(\vec{h}^{i}_{\phi}(x),H_{\phi}(x)))] - \mathbb{E}_{\mathbb{P}\times\tilde{\mathbb{P}}}[\operatorname{sp}(T_{\phi,\psi}(\vec{h}^{i}_{\phi}(x'),G_{\phi}(x)))]$ 

• Where x is an input sample, x' is a negative graph sample,  $sp(z) = log(1 + e^z)$ , T(,) is a neural network



# **InfoGraph\*: Semi-supervised Graph Representation Learning**

- Two objective functions:
  - Supervised loss
  - Unsupervised loss
- Simply combining the two objectives using the same encoder may lead to "negative transfer"
  - The two objectives may favor different information

$$L_{\text{total}} = \sum_{i=1}^{|\mathbb{G}^{L}|} L_{\text{supervised}}(y_{\phi}(G_{i}), o_{i}) + \lambda \sum_{j=1}^{|\mathbb{G}^{L}| + |\mathbb{G}^{U}|} L_{\text{unsupervised}}(h_{\phi}(G_{j}); H_{\phi}(G_{j}))$$

# **InfoGraph\*: Semi-supervised Graph Representation Learning**

- Two different encoders for the supervised and unsupervised tasks
- Maximize the mutual information of the representations learned by the two encoders at all levels (or layers)



# **Results on Graph Classification and Regression**

OMR

 $39.55 \pm 0.22$ 

 $41.01\pm0.17$ 

 $46.06\pm0.21$ 

 $41.27 \pm 0.18$ 

> 1 Day

 $50.68 \pm 0.26$ 

 $55.60 \pm 0.22$ 

 $65.87 \pm 0.98$ 

 $72.30 \pm 3.44$ 

 $66.96 \pm 0.56$ 

 $66.55 \pm 0.25$ 

 $34.65\pm0.19$ 

 $37.99 \pm 0.30$ 

 $43.89 \pm 0.38$ 

 $46.95\pm0.46$ 

 $44.55\pm0.52$ 

 $41.17\pm0.03$ 

Dataset	MUTAG	PTC-MR	RDT-B	RDT-M5K	IMDB-B	IMDB-M
(No. Graphs)	188	344	2000	4999	1000	1500
(No. classes)	2	2	2	5	2	3
(Avg. Graph Size)	17.93	14.29	429.63	508.52	19.77	13.00

Graph Kernels

OMR

 $64.11 \pm 0.14$ 

 $77.34 \pm 0.18$ 

 $68.82 \pm 0.41$ 

 $78.04 \pm 0.39$ 

RW [14]

GK 55

WL 54

DGK 68

MLG 28

SP 3

 $83.72 \pm 1.50$ 

 $85.22 \pm 2.43$ 

 $81.66 \pm 2.11$ 

 $80.72\pm3.00$ 

 $87.44 \pm 2.72$ 

 $87.94 \pm 1.61$ 

 $57.85 \pm 1.30$ 

 $58.24 \pm 2.44$ 

 $57.26 \pm 1.41$ 

 $57.97 \pm 0.49$ 

 $60.08 \pm 2.55$ 

 $\mathbf{63.26} \pm \mathbf{1.48}$ 

Table 1: Graph classification accuracy with unsupervised methods

 .48
 > 1 Day

 Other Unsupervised Methods

node2vec [17]	$72.63 \pm 10.20$	$58.58 \pm 8.00$	-	-	-	-
sub2vec 👖	$61.05 \pm 15.80$	$59.99 \pm 6.38$	$71.48 \pm 0.41$	$36.68 \pm 0.42$	$55.26 \pm 1.54$	$36.67\pm0.83$
graph2vec 38	$83.15 \pm 9.25$	$60.17 \pm 6.86$	$75.78 \pm 1.03$	$47.86 \pm 0.26$	$71.1 \pm 0.54$	$50.44 \pm 0.87$
InfoGraph	$89.01 \pm 1.13$	$61.65 \pm 1.43$	$82.50 \pm 1.42$	$53.46 \pm 1.03$	$73.03 \pm 0.87$	$49.69 \pm 0.53$

Target	Mu (0)	Alpha (1)	HOMO (2)	LUMO (3)	Gap (4)	R2 (5)	ZPVE(6)	U0 (7)	U (8)	H (9)	G(10)	Cv (11)
MAE	0.3201	0.5792	0.0060	0.0062	0.0091	10.0469	0.0007	0.3204	0.2934	0.2722	0.2948	0.2368
Semi-Supervised						Error Ratio	)					
Mean-Teachers	1.09	1.00	0.99	1.00	0.97	0.52	0.77	1.16	0.93	0.79	0.86	0.86
InfoGraph	1.02	0.97	1.02	0.99	1.01	0.71	0.96	0.85	0.93	0.93	0.99	1.00
InfoGraph*	0.99	0.94	0.99	0.99	0.98	0.49	0.52	0.44	0.58	0.57	0.54	0.83

Table 2: Results of semi-supervised experiments on QM9 data set.

#### **Research Problems**



#### **Molecule Generation and Optimization**

#### • Deep generative models for data generation



Image generation (by StyleGAN, From Internet)



Text generated by by GPT-2 Examples from Internet



Graphs?

#### **GraphAF: an Autoregressive Flow for Molecular Graph Generation (Shi & Xu ICLR'20)**

- Formulate graph generation as a sequential decision process
  - In each step, generate a new atom
  - Determine the bonds between the new atoms and existing atoms



Chence Shi, Minkai Xu, Zhaocheng Zhu, Weinan Zhang, Ming Zhang, and Jian Tang. "GraphAF: a Flow-based Autoregressive Model for Molecular Graph Generation." ICLR'20.

# Normalizing Flows (Dinh et al. 2016)

• Defines an invertible mapping from a base distribution (e.g. Gaussian Distribution) to observation space  $f: z \to x$ 



Change-of-Variables

$$p_{\chi}(x) = p_{Z}\left(f_{\theta}^{-1}(x)\right) \left| \det \frac{\partial f_{\theta}^{-1}(x)}{\partial x} \right|$$

**Density estimation using Real NVP** (2016)

# **GraphAF: an Autoregressive Flow for Molecular Graph Generation**

- Traverse a graph through BFS-order
  - Transform each graph into a sequence of nodes and edges
- Defines an invertible mapping from a base distribution (Gaussian distribution) to the observations (graph nodes and edge sequences)





# **Advantages of GraphAF**

- Strong capacity for data density modeling
  - Thanks to normalizing flow-based framework
- Training (from z to  $\epsilon$ ): parallel
  - Efficient training process
- Sampling (from  $\epsilon$  to z): sequential
  - Effectively capture the graph structure
  - Feasible to incorporate chemical rules



(b) Autoregressive Flow

#### **Molecule Generation**

- Training Data: ZINC250K
  - 250K drug-like molecules with a maximum atom number of 38
  - 9 atom types and 3 edge types

Method	Validity	Validity w/o check	Uniqueness	Novelty	Reconstruction	
JT-VAE	100%	_	$100\%^{\ddagger}$	$100\%^{\ddagger}$	76.7%	-
GCPN	100%	20%	<b>99.97%</b> <sup>‡</sup>	100%*-		!
MRNN	100%	65%	99.89%	100%		
GraphNVP	42.60%	<u> </u>	94.80%	100%	100%	
GraphAF	100%	68%	99.10%	100%	100%	_

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# **Goal-Directed Molecule Generation with Reinforcement Learning**

- Fine tune the generation policy with reinforcement learning to optimize the properties of generated molecules
- State: current subgraph *G<sub>i</sub>*
- Action: generating a new atom (i.e.  $p(X_i|G_i)$ ) or a new edge  $(p(A_{ij}|G_i, X_i, A_{i,1:j-1})).$
- **Reward Design**: the properties of molecules (final reward) and chemical validity (intermediate and final reward)

## **Molecule Optimization**

- Properties
  - Penalized logP
  - QED (druglikeness)

Mathad		Penali	zed logP		QED				
Method	1st	2nd	3rd	Validity	1st	2nd	3rd	Validity	
ZINC (Dataset)	4.52	4.30	4.23	100.0%	0.948	0.948	0.948	100.0%	
JT-VAE (Jin et al., 2018)	5.30	4.93	4.49	100.0%	0.925	0.911	0.910	100.0%	
GCPN (You et al., 2018a)	7.98	7.85	7.80	100.0%	0.948	0.947	0.946	100.0%	
MRNN <sup>1</sup> (Popova et al., 2019)	8.63	6.08	4.73	100.0%	0.844	0.796	0.736	100.0%	
GraphAF	12.23	11.29	11.05	100.0%	0.948	0.948	0.947	100.0%	



#### **Constrained Optimization**





-14.32 3.58 (c) Constrained optimization

#### **Research Problems**



## **Retrosynthesis Prediction**

- Once a molecular structure is designed, how to synthesize it?
- Retrosynthesis planning/prediction
  - Identify a set of reactants to synthesize a target molecule



# A Graph to Graphs Framework for Retrosynthesis Prediction (Shi et al. 2020)

- Each molecule is represented as a molecular graph
- Formulate the problem as a graph (product molecule) to a set of graphs (reactants)
- The whole framework are divided into two stages
  - Reaction center identification
  - Graph Translation

Chence Shi, Minkai Xu, Hongyu Guo, Ming Zhang and Jian Tang. A Graph to Graphs Framework for Retrosynthesis Prediction. ICML, 2020.

#### The G2Gs Framework (Shi et al. 2020)



Shi et al., 2020, A Graph to Graphs Framework for Retrosynthesis Prediction

#### **Reaction Center Prediction**

- An atom pair (*i*, *j*) is a reaction center if:
  - There is a bond between atom *i* and atom *j* in product
  - There is no bond between atom *i* and atom *j* in reactants
- A supervised classification problem
  - Encode each edge with a graph neural network



## **Graph Translation**

- Translate the incomplete synthon to the final reactant
- A variational graph to graph framework
  - A latent variable z is introduced to capture the uncertainty during translation



# **Experiments**

- Experiment Setup
  - Benchmark data set USPTO-50K, containing 50k atom-mapped reactions
  - Evaluation metrics: top-k exact match (based on canonical SMILES) accuracy

Table 1. Top-k exact match accuracy when reaction class is given. Results of all baselines are directly taken from (Dai et al., 2019).

Table 2. Top-k exact match accuracy when reaction class is unknown. Results of all baselines are taken from (Dai et al., 2019).

Methods	Top- $k$ accuracy %				Methods	Top- $k$ accuracy %				
	1	3	5	10	Wiethous	1	3	5	10	
Template-free					Template-free					
Seq2seq G2Gs	37.4 <b>61.0</b>	52.4 <b>81.3</b>	57.0 <b>86.0</b>	61.7 <b>88.7</b>	Transformer G2Gs	37.9 <b>48.9</b>	57.3 <b>67.6</b>	62.7 <b>72.5</b>	/ 75.5	
Template-based						Templ	ate-based			
Retrosim Neuralsym GLN	52.9 55.3 <b>64.2</b>	73.8 76.0 <b>79.1</b>	81.2 81.4 <b>85.2</b>	88.1 85.1 <b>90.0</b>	Retrosim Neuralsym GLN	37.3 44.4 <b>52.5</b>	54.7 65.3 <b>69.0</b>	63.3 72.4 <b>75.6</b>	74.1 78.9 <b>83.7</b>	

# **Going Beyond 2D Graphs: 3D Structures**

- A more natural and intrinsic representations of molecules: 3D conformations
  - Determines its biological and physical activities
  - E.g., charge distribution, steric constraints, and interaction with other molecules



## **Conformation Prediction**

- For most molecules, their 3D structure are not available
- How to predict valid and stable conformations?
  - Each atom is represented as its 3D coordinates



# **Traditional Approaches**

- Experimental methods
  - Crystallography
  - Expensive and time consuming
- Computational methods
  - Molecular dynamics, Markov chain Monte Carlo
  - Very computational expensive, especially for large molecules

# **Machine Learning Approaches**

- Train a model to predict molecular conformations *R* given the molecular graph *G*, i.e., modeling p(*R*|*G*) (Mansimov et al. 2019, Simm and Hernandez-Lobato 2020)
- Challenges
  - Conformations are rotation and translation equivalent
  - The distribution  $p(\mathbf{R}|\mathcal{G})$  is multimodal and very complex



# **Our Solution (Xu et al. 2020)**

- A flexible generative model  $p_{\theta}(\mathbf{R}|\mathcal{G})$  based on normalizing flows
  - Treating pairwise distances *d* as intermediate variables
  - First generating the distance d based G, i. e.  $p_{\theta}(d|G)$
  - Generating conformations based on d and G, i.e.  $p_{\theta}(\mathbf{R}|\mathbf{d}, G)$

$$p_{\theta}(\boldsymbol{R}|\mathcal{G}) = \int p(\boldsymbol{R}|\boldsymbol{d},\mathcal{G}) \cdot p_{\theta}(\boldsymbol{d}|\mathcal{G}) \,\mathrm{d}\boldsymbol{d}$$

• Further correct  $p_{\theta}(\mathbf{R}|\mathcal{G})$  with an energy-based tilting term  $E_{\phi}(\mathbf{R},\mathcal{G})$ 

$$p_{\sqrt{\varphi}}(R|G) / p_{\sqrt{R}}(R|G) \cdot \exp(-E_{\varphi}(R,G))$$

Minkai Xu\*, Shitong Luo\*, Yoshua Bengio, Jian Peng, Jian Tang. Learning Neural Generative Dynamics for Molecular Conformation Generation. In Submission.

#### **Distance Geometry Generation** $p_{A}(d|G)$

• Conditional Graph Continuous Flow (CGCF)

d

- Defines an invertible mapping between a base distribution and the pairwise atom distance d conditioning on the molecular graph G
- Defines the continuous dynamics of distance *d* with Neural Ordinary Differential Equations (ODEs):

$$F_{\mathcal{A}}(d(t_0), G) = d(t_0) + \begin{bmatrix} z & t_1 \\ t_0 \end{bmatrix} f_{\mathcal{A}}(d(t), t; G) dt, \quad d(t_0) \leftarrow N(0, 1) \\ \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} \\ \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} \\ \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} \\ \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} & \downarrow_{t_0} \\ \downarrow_{t_0} & \downarrow_{t_0} \\ \downarrow_{t_0} & \downarrow_{t_0} &$$

#### **Conformation Prediction** $p(\mathbf{R}|\mathbf{d}, \mathcal{G})$

• Defines the distribution of conformation *R* given the molecular graph *G* and the pairwise atom distance *d* 

$$p(\boldsymbol{R}|\boldsymbol{d}, \mathcal{G}) = \frac{1}{Z} \exp\left\{-\sum_{e_{uv} \in \mathcal{E}} \alpha_{uv} \left(\|\boldsymbol{r}_u - \boldsymbol{r}_v\|_2 - d_{uv}\right)^2\right\}$$

• Trying to find the conformations R that satisfy the distance constraints



# **Energy-based Tilting Model**

• Further correct  $p_{\theta}(\mathbf{R}|\mathcal{G})$  with an energy-based tilting term  $E_{\phi}(\mathbf{R},\mathcal{G})$ 

$$p_{\checkmark,\varphi}(R|G) / p_{\checkmark}(R|G) \cdot \exp(-E_{\varphi}(R,G))$$

- Explicitly learn an energy function  $E_{\phi}(\mathbf{R}, \mathcal{G})$  with SchNet (Schütt et al. 2017)
  - Neural message passing in 3D space



# **Training Energy Model**

- Directly training EBMs with maximum likelihood is difficult
  - Involving a slow sampling process from the model distribution (e.g. with Langevin dynamics)
- Training EBMs with negative sampling
  - Treating observed conformations as positive examples
  - Generating negative conformations through the flow-based model  $p_{\theta}(\boldsymbol{R}|\mathcal{G})$

$$\mathcal{L}_{\text{nce}}(\boldsymbol{R}, \mathcal{G}; \phi) == -\mathbb{E}_{p_{\text{data}}} \left[ \log \frac{1}{1 + \exp(E_{\phi}(\boldsymbol{R}, \mathcal{G}))} \right] - \mathbb{E}_{p_{\theta}} \left[ \log \frac{1}{1 + \exp(-E_{\phi}(\boldsymbol{R}, \mathcal{G}))} \right]$$

# **The Final Sampling Process:**



## Examples

Graph	Conformations										
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# Medical Knowledge Graph Construction (Ongoing)

- >7M Entities, ~300M facts
  - Disease
  - Drug
  - Phenotype
  - Gene
  - Protein
  - Side effect
- Biomedical literature





# **Drug Repurposing with Biomedical Knowledge Graphs (Ongoing)**

- Drug repurposing: identifying effective drugs for a disease from existing approved list
- Predicting the links between diseases and drugs on biomedical knowledge graphs



Figure borrowed from Zeng et al. 2020

#### **Summary**

- Great potential of AI to drug discovery
  - Extracting evidence from a huge amount of biomedical data
- Many data in this domain are graph-structured
  - Molecules, biomedical knowledge graphs
- Great representation learning for drug discovery
  - Molecule properties prediction
  - De novo molecule design and optimization
  - Retrosynthesis prediction
  - Drug repurposing

#### **Future Directions**

- Going beyond from 2D graphs to 3D structures
- Drug Discovery with Limited Labeled Data
  - Active Learning
  - Self-supervised Learning
  - Multi-task/Transfer Learning
  - Few-shot Learning

# AAAI'21 Tutorial on Artificial Intelligence for Drug Discovery

- Date: 8:30 am 11:45 am, Feb. 03, 2021
- Speakers



Jian Tang Mila-Quebec Al Institute



Fei Wang Weill Cornell Medicine



Feixiong Cheng Cleveland Clinic

#### Thanks!

- Current Students
  - Meng Qu
  - Zhaocheng Zhu
  - Andreea Deac
  - Louis-Pascal Xhonneux
  - Shengchao Liu
  - Chence Shi
  - Minkai Xu
- Collaborators and previous students:, Yoshua Bengio, Jian Peng, Fei Wang, Feixiong Cheng, Ming Zhang, Fanyun Sun, Hongyu Guo, Jordan Hoffmann, Vikas Verma,....



#### Microsoft<sup>®</sup> Research







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#### **GraphAF: an Autoregressive Flow for Molecular Graph Generation**

- G=(A, X), where A is the adjacency matrix, X is the atom type
- Dequantize a discrete graph G into continuous data

 $z_i^X = X_i + u, \ u \sim U[0,1)^d; \ z_{ij}^A = A_{ij} + u, \ u \sim U[0,1)^{b+1}$ 

• Define the conditional distributions as:

$$\begin{array}{ll} \text{Node generation:} & p(z_i^X | G_i) = \mathcal{N}(\mu_i^X, (\alpha_i^X)^2), \\ & \text{where } \mu_i^X = g_{\mu^X}(G_i), \alpha_i^X = g_{\alpha^X}(G_i), \\ \text{Edge generation:} & p(z_{ij}^A | G_i, X_i, A_{i,1:j-1}) = \mathcal{N}(\mu_{ij}^A, (\alpha_{ij}^A)^2), \ j \in \{1, 2, \ldots, i-1\}, \\ & \text{where } \mu_{ij}^A = g_{\mu^A}(G_i, X_i, A_{i,1:j-1}), \alpha_{ij}^A = g_{\alpha^A}(G_i, X_i, A_{i,1:j-1}) \\ \end{array}$$

**G**<sub>i</sub>: current graph substructure, encoded with graph neural networks